

- d. Find the vector equation and parametric equations of a line and a plane in \mathbb{R}^3 .
 - e. Solve problems involving linear combinations, linear dependence, linear independence, the span of a set of vectors, bases, and dimension in \mathbb{R}^n .
 - f. Find a basis and the dimension of the column space and the null space of a matrix.
 - g. Understand the connection between bases and coordinate systems and find the coordinates of a vector relative to a given basis.
4. Inner product, length, distance, angle, and orthogonality:
- a. Apply the basic properties of the dot product and use the dot product to solve problems and define the norm of a vector, the angle between two vectors, the distance between two vectors and orthogonality in \mathbb{R}^n .
 - b. Find a linear equation for a plane in \mathbb{R}^3 using a point on the plane and normal vector to the plane.
 - c. Calculate the orthogonal projection of one vector onto another in \mathbb{R}^n .
 - d. Use orthogonal projection to find distance of a point from a line and from a plane in \mathbb{R}^3 .
 - e. Explain the terms standard basis, orthogonal basis and orthonormal basis and be able to convert a basis into an orthonormal basis using the Gram-Schmidt Process (max of three vectors) in \mathbb{R}^n .
 - f. Find the orthogonal projection of a vector y onto a given subspace S of \mathbb{R}^n and find the vector in S that is closest to y .
 - g. Determine the set of least-squares solutions of a given inconsistent linear system.
5. Linear transformations from \mathbb{R}^n to \mathbb{R}^m :
- a. Determine the matrices that describe rotation, shear, dilation or contraction and reflection in \mathbb{R}^2 .
 - b. Matrix transformations, domain, codomain, standard matrix, kernel, range, one-to-one, onto, linearity. Explain these terms in terms of rotation, reflection, etc.
 - c. Determine whether a given transformation from \mathbb{R}^n to \mathbb{R}^m is linear.
 - d. Determine the standard matrix for a linear transformation from \mathbb{R}^n to \mathbb{R}^m .
 - e. Form composite of linear transformations.
 - f. Determine the kernel, range, rank, and nullity of a linear transformation.
 - g. Determine if a linear transformation is one-to-one.
 - h. Determine if a linear transformation is onto.
 - i. Determine if a linear transformation is invertible, and if it is, find its inverse.
6. Determinants:
- a. Calculate determinants using row operations, column operations, and expansion down any column and across any row.
 - b. Solve a system using Cramer's Rule.
 - c. Find the inverse of a matrix using the adjoint of the matrix.
 - d. Find the volume of a parallelepiped.
 - e. Prove and apply the basic properties of the determinant of a matrix.
 - f. Prove and apply the basic properties of the cross product and use the cross product to calculate the area of a triangle and the volume of a parallelepiped.

7. Eigenvalues and eigenvectors:

- a. Find the characteristic polynomial, eigenvalues and eigenspaces of a square matrix and determine whether the matrix is diagonalizable.
- b. Find the powers of a diagonalizable matrix.
- c. Solve problems in population dynamics.
- d. Solve linear systems of differential equations.

8. Proofs:

- a. Be able to put together a mathematical argument to prove simple facts about vectors, matrices, determinants, dot products, length, projection, linear independence, subspaces and linear transformations.

INSTRUCTION AND GRADING

Instructional (Contact) Hours:

Type	Duration
Lecture	39
Seminars/Tutorials	
Laboratory	
Field Experience	
Other (<i>specify</i>):	
Total	39

Grading System: Letter Grades Percentage Pass/Fail Satisfactory/Unsatisfactory Other

Specify passing grade: 50%

Evaluation Activities and Weighting (total must equal 100%)

Assignments: 10% <i>Specify number of, variety, and nature of assignments:</i>	Lab Work: %	Participation: % <i>Specify nature of participation:</i>	Project: % <i>Specify nature of project:</i>
Quizzes/Test: 10%	Midterm Exams: 40%	Final Exam: 40%	Other: % <i>Specify:</i>

TEXT(S) AND RESOURCE MATERIALS

Provide a full reference for each text and/or resource material and include whether required/not required.

Linear Algebra and its Applications, Latest edition, David C. Lay, Pearson Addison Wesley.

COURSE TOPICS

List topics and sequence covered.

Week	Topic
Week 1	Matrices, matrix addition, scalar multiplications, transpose, linear combinations, matrix equations, applications. Row-column product and general matrix product, matrix vector product and its relation to linear combinations and linear systems, properties of matrix multiplication.
Week 2	Matrix multiplication continued, Vectors in R^2 and R^3 , geometric method of vector addition, subtraction, scalar multiplication, linear combinations, span. Subspaces of R^2 and R^3 . Vector equation and parametric equations of lines and planes.
Week 3	Inner product, length, distance, angle and orthogonality, Scalar equation of a plane, projection, distance of a point from a line/plane, orthogonal and orthonormal sets of vectors.
Week 4	Matrix transformations: determine the matrices that describe rotation, shear, dilation or contraction and reflection in R^2 . Explain the terms domain, codomain, standard matrix, kernel, range, one-to-one, onto, linearity in terms of these transformations. Standard matrix for a linear transformation from R^n to R^m . Composite of linear transformations. Transformations continued. Midterm 1 Solving linear systems by row-reduction, existence and uniqueness of solutions, rank of a matrix.
Week 5	Transformations continued. MIDTERM 1
Week 6	Solving linear systems by row-reduction, existence and uniqueness of solutions, rank of a matrix.
Week 7	Applications of systems: polynomial interpolation, balancing chemical equations, Leontieff's exchange model, network flow.
Week 8	Applications of systems: find the inverse of a matrix; solve problems involving linear combinations, subspaces of R^n , linear dependence / independence, kernel and range of linear transformations, conditions for being 1-1, onto, invertible, inverse of a linear transformation.
Week 9	Applications continued. Basis and dimension: row space, column space and null space of a matrix, subspaces of R^n , coordinates of a vector relative to a basis.
Week 10	Calculate determinants using cofactor expansion, row operations and column operations, properties of determinants. MIDTERM 2
Week 11	Determinants continued. Applications of determinants: Cramer's rule, adjoint formula for matrix inverse, area and volume.

Week 12	Eigenvalues and eigenspaces of a square matrix, diagonalization of a square matrix, applications of diagonalization.
Week 13	Gram-Schmidt process for finding an orthonormal basis for a subspace coordinates relative to an orthogonal basis. Determine the set of least-squares solutions of a given inconsistent linear system.
Week 14	FINAL EXAM

NOTES

1. Students are required to follow all College policies. Policies are available on the website at: [Coquitlam College Policies](#)
2. To find out how this course transfers, visit the BC Transfer Guide at: bctransferguide.ca